

Problem Set 5

Prof. Oke

CEE 260/MIE 273: Probability & Statistics in Civil Engineering

9.29.2025

Due Tuesday, October 13, 2026 at 12:59 PM as PDF uploaded via Gradescope. Use this document as your template. **Show as much work as possible in order to get FULL credit.** There are 7 problems with a total of 41 points available. **Important:** If you use Python for any probability computations, briefly write/include the statements you used to arrive at your answers. If instead you use probability tables or a calculator, note this in the respective solution, as well.

Problem 1 (4 points)

Respond “T” (True) or “F” (False) to the following statements. Use the boxes provided. Each response is worth 1 point.

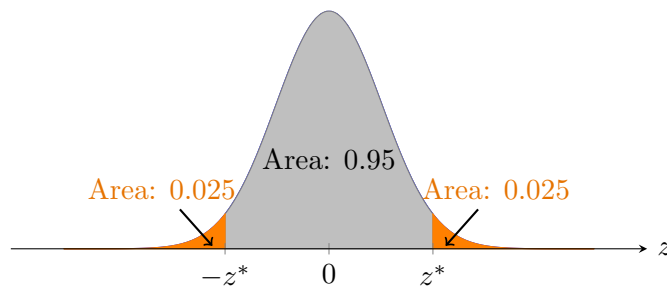
- (a) ☐ If the natural logarithm of a random variable is normally distributed with parameters μ and σ , then the variable is lognormally distributed with the same parameters.
- (b) ☐ The mean of a lognormal distribution is equal to or greater than its median.
- (c) ☐ The mean of a exponentially-distributed random variable is equal to the inverse of its variance.
- (d) ☐ A binomial distribution with sufficiently large n can be approximated by a normal distribution with $\mu = np$.

Problem 2: Normal and Lognormal Distributions (6 points)

Choose the option that best fills in the blank.

[1]

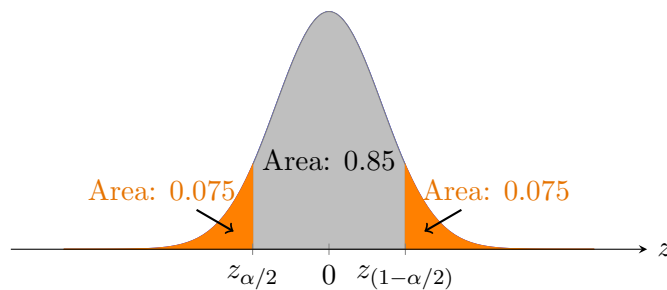
- (a) The figure below depicts the PDF of a standard normal distribution. What is the value of z^* in the figure?



- (i) 0
- (ii) 1.65
- (iii) 1.96
- (iv) 2.58

[1]

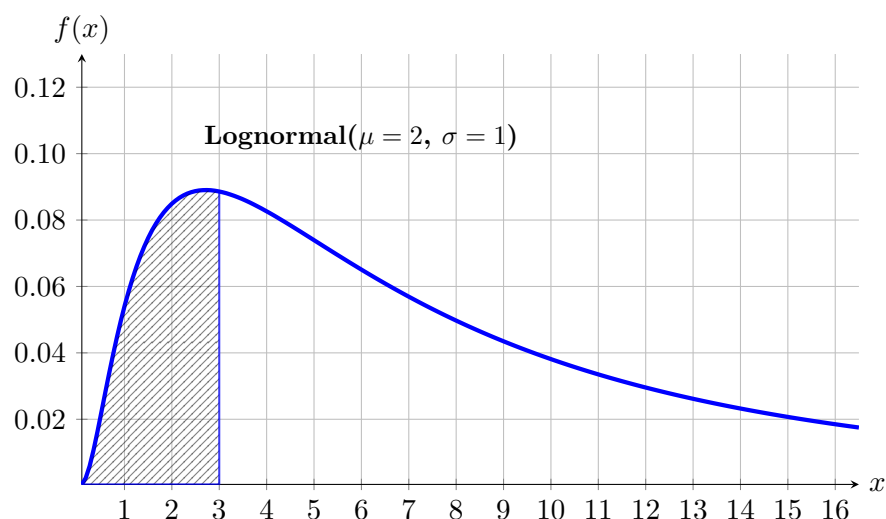
- (b) The figure below depicts the PDF of a standard normal distribution. What is the value of $z_{\alpha/2}$ in the figure?



- (i) 0
- (ii) -1.04
- (iii) -1.28
- (iv) -1.44

[2]

- (c) Find the area of the shaded portion in the figure below.



Answer:

Problem 3: Lognormal Distribution (*6 points*)

Given that the lifetime in days of an electronic component is lognormally distributed with $\mu = 1.1$ and $\sigma = 0.5$.

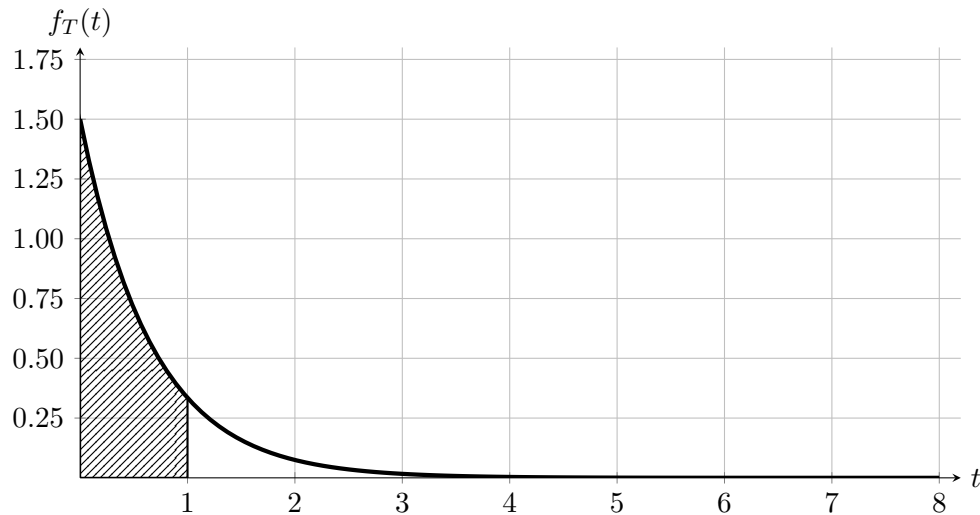
(a) Find the median lifetime of the component. [1]

(b) Find the mean lifetime of the component. [2]

(c) Find the probability that a component lasts between 3 and 5 days. [3]

Problem 4: Exponential Distribution I (4 points)

- [1] (a) The graph below is the PDF of an exponentially distributed random variable T , given by $f_T(t) = \lambda e^{-\lambda t}$. What is the value of the parameter λ ?



Answer:

- [1] (b) What is the mean of T ?

Answer:

- [2] (c) What is the probability represented by the shaded area in the figure in part (i)? (A numeric value is expected here, not just a symbolic expression.)

Answer:

Problem 5: Exponential Distribution II *(7 points)*

The delay time T of a flight is exponentially distributed with $\lambda = 4$ (mean rate of occurrence per hour).

- (a) What is the expectation of T ? [1]

- (b) What is the standard deviation of T ? [1]

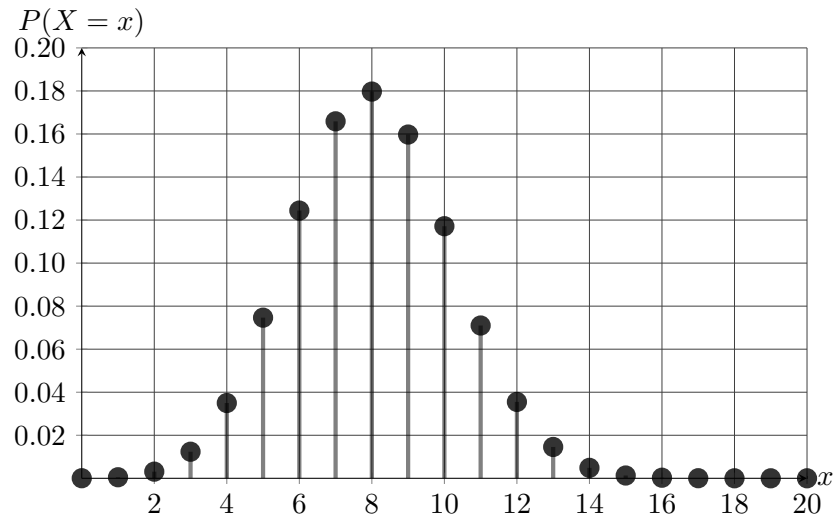
- (c) What is the probability that a flight is delayed by no more than half an hour? [2]

- (d) Given that a family member has already waited for half an hour, what is the probability that a certain flight will be further delayed by over an hour? [3]

Problem 6: Binomial Distribution I (6 points)

Show brief amount of work for partial credit if answer is wrong. Not required however for full credit.

The PMF of a random variable X is given in the figure below.



- [1] (a) Use the figure to estimate the probability $P(X = 8)$.

Answer:

- [2] (b) Use the figure to estimate the probability $P(X = 8 \cup X = 10)$.

Answer:

- [2] (c) Use the figure to estimate the probability $P(5 < X \leq 8)$.

Answer:

- [1] (d) If the PMF in the figure above is that of a Binomial distribution with $p = 0.4$, what is $E(X)$?

Answer:

Problem 7: Binomial Distribution II (8 points)

75% of all vehicles examined at an emissions inspection station pass. Successive vehicles pass or fail independently of one another. Let X be the number of vehicles that pass the inspection out of the next $n = 6$ vehicles inspected.

- (a) What is the expectation of X , i.e. $\mathbb{E}[X]$? [1]
- (b) What is the standard deviation of X ? [1]
- (c) Find the probability that all of the next six vehicles inspected pass, i.e. $P(X = 6)$. [1]
- (d) Find the probability that only two of the next six vehicles inspected pass, i.e. $P(X = 2)$. [2]
- (e) Find the probability that at least four of the next six vehicles inspected pass. [3]